

# Parallelizing Equation-Based Models for Simulation on Multi-Core Platforms by Utilizing Model Structure

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# Part I

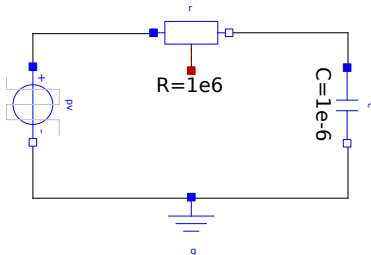
## Background

# Equation-Based Modelling and Simulation

- ▶ Declarative and acausal – describe the problem instead of the solution
- ▶ Symbolic manipulations
- ▶ Numerical methods and solvers

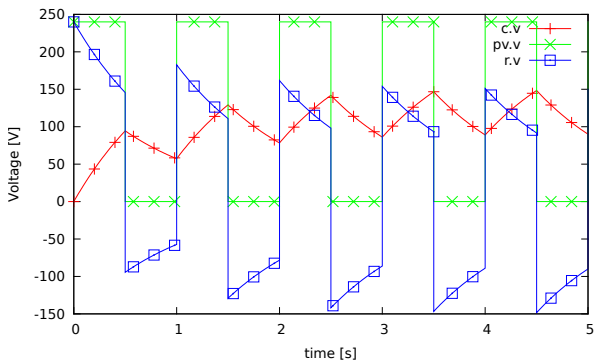
- ▶ An equation-based object-oriented language
- ▶ Primarily used to model and simulate (multi-domain) physical systems
- ▶ Easiest explained through an example

# RC Circuit Example: Different Representations



```
model RC
  import Modelica.Electrical.Analog.Basic;
  import Modelica.Electrical.Analog.Sources;
  Basic.Capacitor c;
  Basic.Resistor r;
  Basic.Ground g;
  Sources.PulseVoltage pv;
equation
  connect(pv.n,g.p);
  connect(r.p,pv.p);
  connect(g.p,c.n);
  connect(r.n,c.p);
end RC;
```

# RC Circuit Example: Results



**Figure:** Simple RC circuit simulation with input square wave pv.v, capacitor voltage c.v, and resistor voltage r.v.

# Sorting and Matching

- ▶ There exists many valid solution paths
  - ▶  $v = r * i$
  - ▶  $i = v/r$
  - ▶  $r = v/i$
  - ▶ ...
- ▶ We will not use an integrated approach
  - ▶ Normal sorting+matching, then parallelize
  - ▶ Parallelize, then sort+match

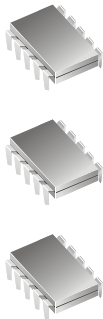
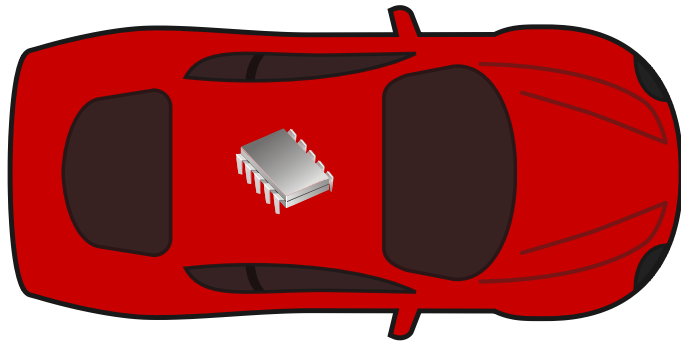
- ▶ Open source Modelica tool
- ▶ Open Source Modelica Consortium (OSMC)
  - ▶ Many partners
  - ▶ Main development at Linköping University
- ▶ Used for research prototypes and industrial products



# Part II

## Parallelisation of Equation-Based Models

# Single-Core Solution



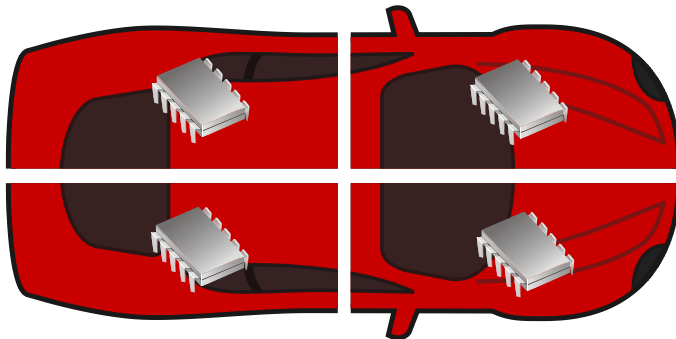
# Where Should You Parallelise?

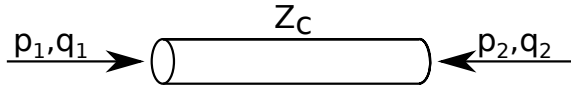
- ▶ Expression level
- ▶ Equation blocks
- ▶ The ODE solver
- ▶ The simulation itself

# Where Should You Parallelise?

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# Multi-Core Solution

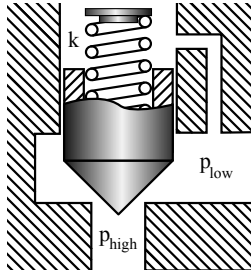




**Figure:** Transmission line components calculate wave propagation through a line using a physically correct separation in time.

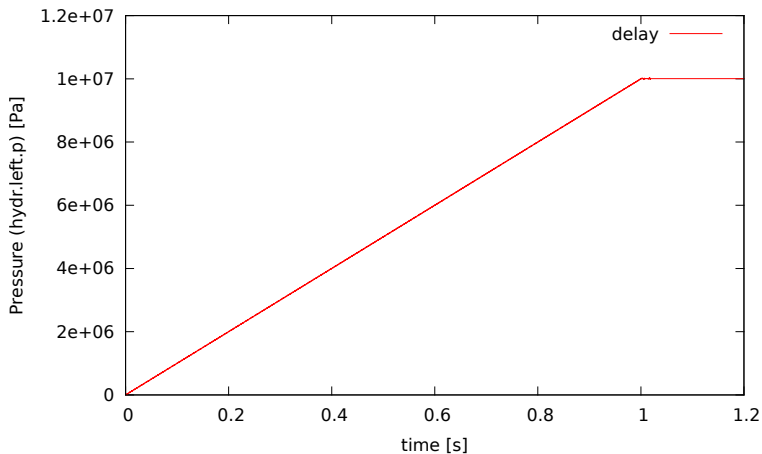
## Implementing the delay line: Delay

```
left.c = delay(right.c + 2*Zc*right.q, T);  
right.c = delay(left.c + 2*Zc*left.q, T);
```



**Figure:** A pressure relief valve is designed to protect a hydraulic system by opening at a specified maximum pressure.





**Figure:** Pressure increases until the reference pressure of 10 MPa is reached, where the relief valve opens.

# Preparing for Parallelization

- ▶ Thread pooling in OpenMP
- ▶ Thread safety in the run-time system
- ▶ Partitioning the system into parallel parts

$$\begin{bmatrix} * & & & & \\ * & * & & & \\ & X & * & & \\ & & * & * & \\ & & & * & * \\ & & & & * \end{bmatrix}$$

(a) Regular system

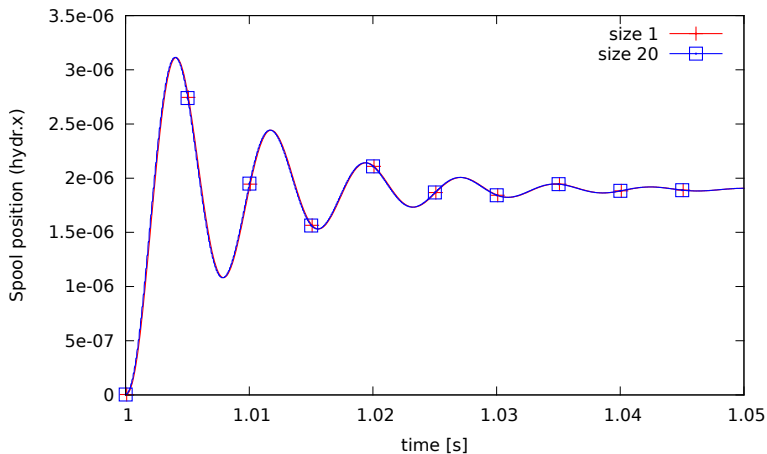
$$\begin{bmatrix} * & & & & \\ * & * & & & \\ & & * & & \\ & & * & * & \\ & & * & & * \\ & & & & * \end{bmatrix}$$

(b) TLM system

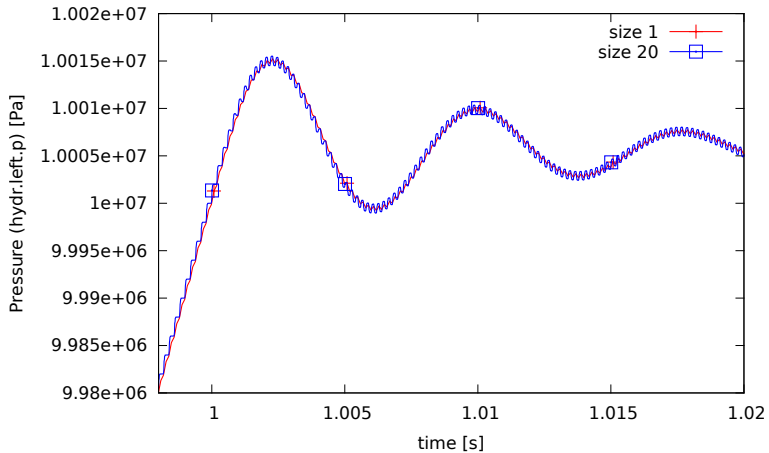
$$\begin{bmatrix} * \\ * \end{bmatrix} \begin{bmatrix} * & & \\ * & * & \\ * & & * \end{bmatrix}$$

(c) Partitioned systems

Figure: Adjacency matrices in lower triangular form.



**Figure:** Comparison of spool position using a volume split into more segments.



**Figure:** Comparison of system pressure using a volume split into more segments.

# Performance Improvements from Parallel Simulation

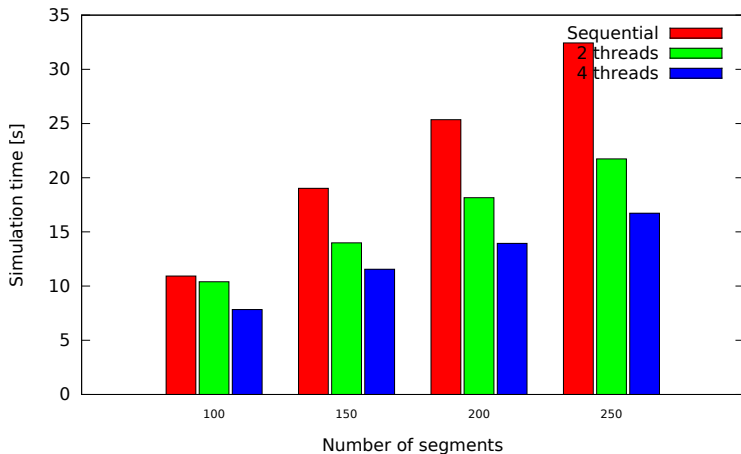


Figure: Simulation time vs. number of segments.

# Part III

## Conclusion

# Summary

- ▶ TLM has been used to introduce parallelism in an example model
- ▶ Running models in parallel gives performance improvement using OpenMP



# Future Work

- ▶ Optimise operators (delay) for parallel simulation
- ▶ Merge small tasks
- ▶ Schedule parallel tasks better
- ▶ Add more parallelisation schemes
- ▶ Add profiling for parallel simulation (waiting times, etc)



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